## Englewood Public School District <br> Mathematics <br> Grade 7 <br> Fourth Marking Period

## Unit - Area, Volume and Statistics

Overview: During this unit, students will learn about circumference and area of a circle, surface area and volume of a prism, area of composite figures, statistics and probability.

Time Frame: Chapter 8 (8.1 \& Online CC Additional Resources) - 14 days, Chapter 9 - 14 days, Chapter 10 ( \& Online Common Core Additional Resources) - 14 days

## Enduring Understandings:

The area of a polygon can be found by dividing it into smaller shapes, and then addition the areas of those shapes.
A circle is a geometric figure that has many useful applications in the real world.
Measures of central tendency and measures of variation are used to draw conclusions about populations.
Events happen around you every day, some more likely than others.
You can use probability to describe how likely an event is to occur.

## Essential Questions:

How can the formulas for area and circumference of a circle be derived and used to solve problems?
How can the properties of angles be used to solve multi-step problems?
How can area, surface area, and volume be used to solve problems?
What two-dimensional figures be formed by slicing a three-dimensional figure?
How can random sampling be used to gain and generalize information about a population?
How does generating multiple random samples assist in drawing inferences about a population?
How can data distributions be used to measure variability?
How can the measures of center and variability be used to compare two populations?
How is the likelihood of an event expressed as a probability?
How can probability be used to approximate the frequency of a chance event?
How can probability be used to make predictions about uncertain events?

| Standards | Topics and Objectives | Activities |  | Resources | Assessments |
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| Chapter 8 |  |  |  |  |  |
| (8.1 Only \& Online CC |  |  |  |  |  |
| Additional Resources) |  |  |  |  |  |
| Note: | Topics | 7.G.A.3 Cube Ninjas! | SE-7B: 120-132 | Unit 4 Benchmark |  |


|  | - Area of composite figures. <br> - Radius, diameter and circumference of a circle. <br> - Area of a circle. <br> - Real-world problems involving area and circumference of circles, semicircles, quadrants and composite figures. <br> - Real-world problems involving surface area and volume of prisms. <br> - Recognizing cylinders, cones, spheres and pyramids. <br> Twenty-First Century Themes and Skills include: <br> - Creativity and <br> Innovation <br> - Critical Thinking and <br> Problem Solving <br> - Communication and Collaboration <br> Objectives <br> The students will be able to: <br> - Recognize that a plane figure is made up of polygons. <br> - Solve problems involving area of composite figures. <br> - Identify parts of a circle. <br> - Recognize that a circle's |  |  | e |
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| the following standards |  | 7.G.B. 4 Wedges of | Online Common Core Additional Resources | Exact Path |
| in |  |  |  | Summative Assessments: |
| and ar |  | 7.G.B. 4 Eight Circl |  |  |
| located in the Online |  |  | Composite Figures | Math in Focus |
| Common Core Additiona |  | 7.G.B.6, 7.RP.A. 3 Sand under the Swing Set |  | Ass |
| Resources. |  |  |  |  |
| 7.G.A.3. Describe the twodimensional figures that result from slicing threedimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids. |  | Math Playground http://www.mathplaygrou nd.com/ |  | tional Resources for |
|  |  |  |  | Course 2: |
|  |  |  | Diam | Assessments |
|  |  |  | Circumference | ter |
|  |  | Math Fact Practice http://www.playkidsgam es.com/games/mathfact/ mathFact.htm | Circl | Test A, Items: 1-9; Test B, Items: 1-9 |
|  |  |  | Online Common Core Additional Resources for Course 2: | Online Common Core Additional Resources for |
| 7.G.B.4. Know the formulas for the area and circumference of a circle and solve problems; give an informal derivation of the relationship between the circumference and area of a circle. |  | Grades 6-8 Math <br> Fluency Support https://www.engageny.org /resource/mathematics-fluency-support-grades-68 | 11.2 Area of a Circle |  |
|  |  |  | Online CCSS | Area and Volum |
|  |  |  | Additional Resources | Sol |
|  |  |  | C | Review/Te |
|  |  |  | 11.3 Real-Wor | Items: 11-1 |
|  |  | Brain Genie http://braingenie.ck12.org/ | online Common Core | Online Common Core Additional Resources for |
| 7.G.B.6. Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. |  | Math Game Time <br> http://www.mathgametim e.com/ | for Course | Course 2: <br> Assessmen |
|  |  |  | 12.4 Real-W | Chapter 12 |
|  |  |  | oblems: Surfa | Test A, Items: 6-9; |
|  |  | Everything you need to know about math journals: https.//thecornerstoneforte | Area and Volume | Test B, Items: 6-9 |
|  |  |  | Online Common Core <br> Additional Resources for Course 2: | ExamView ${ }^{\circledR}$ Assessment <br> Suite CD-ROM Course 2 |
| Mathematical Practices MP.3, MP.7, MP. 8 |  | achers.com/math-journals/ (NJSLSA.R1, | Chapter 10 Area of Polygons | Formative Assessment <br> Math journal |



|  | surface-area-of-3d-shapes/ <br> (RH.6-8.7) <br> Calculating volume of 3D shapes: <br> https://www.scholastic.co m/teachers/sponsored-content/unexpected-math/17-18/calculating-volume-of-3d-shapes/ (RH.6-8.7) <br> 13 Rockin' volume of pyramids and prisms activities (includes descriptions of activities) https://ideagalaxyteacher.c om/volume-of-pyramids-and-prisms-activities/ (RH.6-8.7) <br> Additional texts: www.newsela.com www.readworks.org www.commonlit.org | - CCSS Lesson Plan: Circular Thinking: Discovering the Area Formula for Circles <br> - CCSS Lesson Plan: Discovering pi <br> - CCSS Prescriptive Lesson Plan: Area and Circumference of a Circle <br> - CCSS Prescriptive Lesson Plan: Surface Area and Volume <br> $7^{\text {th }}$ grade assessments, interactive, videos, games, lessons, homework: https://www.opened.com/sea rch?area=mathematics\&grad e=7\&offset=0\&resource_typ e=interactive-assessment <br> (CRP2, CRP4, CRP8, 8.1.8.A.1) <br> $7^{\text {th }}$ grade worksheets, games, lessons, activities: https://www.education.com/r esources/math/middleschool/ (CRP2, CRP4, CRP8, 8.1.8.A.1) <br> $7^{\text {th }}$ grade common core worksheets: <br> https://www.ixl.com/math/gr ade-7 <br> (CRP2, CRP4, CRP8) |
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|  |  |  | Khan Academy - videos, <br> lessons, assessments |  |
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| from the book; predict the winner of a school election based on randomly sampled survey data. Gauge how far off the estimate or prediction might be. <br> 7.SP.B.3. Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability. For example, the mean height of players on the basketball team is 10 cm greater than the mean height of players on the soccer team, about twice the variability (mean absolute deviation) on either team; on a dot plot, the separation between the two distributions of heights is noticeable. <br> 7.SP.B.4. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. For example, decide whether the words in a chapter of a seventh-grade science book are generally longer than the | samples. <br> - Understand and apply different random sampling methods. <br> - Simulate random sampling. <br> - Make and use inferences about a population to estimate its population mean. <br> - Make comparative inferences about two populations. <br> - Reinforce, consolidate, and extend chapter skills and concepts. | Brain Genie http://braingenie.ck12.org/ <br> Math Game Time http://www.mathgametim e.com/ <br> Everything you need to know about math journals: <br> https://thecornerstoneforte achers.com/math-journals/ <br> (NJSLSA.R1, <br> NJSLSA.W2, <br> NJSLSA.L1) <br> Stem and leaf plots interactive lesson: http://www.shodor.org/int eractivate/lessons/StemAn dLeafPlots/ <br> (RH.6-8.7, 8.1.8.A.1) <br> Stem and leaf plot video: https://www.khanacademy .org/math/ap- <br> statistics/quantitative-data-ap/histograms-stem-leaf/v/u08-l1-t2-we3-stem-and-leaf-plots (CRP2, CRP8) <br> Random sampling and estimation - lake <br> Victoria: https://wvia.pbslearningm edia.org/resource/mgbh.m | Math Goodies - Math <br> Lessons <br> http://www.mathgoodies.co $\underline{\mathbf{m} /}$ <br> $7^{\text {th }}$ grade assessments, interactive, videos, games, lessons, homework: https://www.opened.com/sea rch?area=mathematics\&grad e=7\&offset=0\&resource_typ e=interactive-assessment <br> (CRP2, CRP4, CRP8, <br> 8.1.8.A.1) <br> $7^{\text {th }}$ grade worksheets, games, lessons, activities: <br> https://www.education.com/r esources/math/middleschool/ <br> (CRP2, CRP4, CRP8, <br> 8.1.8.A.1) <br> $7^{\text {th }}$ grade common core worksheets: <br> https://www.ixl.com/math/gr ade-7 <br> (CRP2, CRP4, CRP8) <br> Khan Academy - videos, lessons, assessments www.khanacademy.org (8.1.8.A.1) | Multiple choice / short answer assessments (CRP8) <br> Mini quizzes - assess just one topic, or what was done within 1 or 2 days (CRP8) <br> Alternative Assessments: <br> Learning centers: each learning center focuses on a different type of problem (CRP8) <br> (9.2.8.B.3) <br> Create posters illustrating the main objectives of the unit <br> (RH.6-8.7) <br> Create a dictionary defining and illustrating vocabulary terms (RH.6-8.7) |
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| words in a chapter of a fourth-grade science book. <br> Mathematical Practices MP.1, MP.2, MP.3, MP.4, MP. 8 |  | ath.sp.victoria/random-sampling-and-estimation-lake-victoria (CRP6, CRP8) <br> Random sampling - how many fish? <br> https://wvia.pbslearningm edia.org/resource/mgbh.m ath.sp.fishsample/random-sampling-how-many-fish (CRP6, CRP8) <br> Additional texts: <br> www.newsela.com <br> www.readworks.org <br> www.commonlit.org |  |  |
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| Chapter 10 |  |  |  |  |
| Note: <br> It is recommended that additional lessons be taught for the following standards. The lessons are listed in the Resources column and are located in the Online Common Core Additional Resources. <br> 7.SP.C.5. Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring. Larger numbers indicate greater likelihood. A probability near 0 | Topics <br> Probability, defining outcomes, events, and sample space, finding probability of events, approximating probability and relative frequency and developing probability models. <br> Twenty-First Century Themes and Skills include: <br> - Creativity and Innovation <br> - Critical Thinking and Problem Solving <br> - Communication and Collaboration | 7.SP.C. 6 Heads or Tails <br> 7.SP.C.7, 6 Rolling Dice <br> 7.SP.C.7a How Many <br> Buttons <br> 7.SP.C. 8 Tetrahedral Dice <br> 7.SP.C. 8 Waiting Times <br> Math Playground http://www.mathplaygrou nd.com/ <br> Math Fact Practice http://www.playkidsgam es.com/games/mathfact/ | SE-7B: 240-303 <br> Online Common Core Additional Resources for Course 2: <br> 11.1 Compound Events <br> Online Common Core Additional Resources for Course 2: <br> 11.2 Probability of Compound Events <br> Online Common Core Additional Resources for Course 2: <br> 11.3 Independent | Summative Assessments: <br> Math in Focus Assessments <br> SE/TE: pp. 292-273, 294-297, 298-303 <br> Assessments Course 2: <br> Chapter 10 <br> Test A pp. 139-144; <br> Test B pp. 145-149 <br> Assessments Course 2: <br> End-of-Course <br> Test A pp. 150-161; <br> End-of-Course <br> Test B pp. 162-172 |



| selected at random from a | (RH.6-8.7) | Standards Solution |
| :---: | :---: | :---: |
| class, find the probability that |  | Lessons: |
| Jane will be selected and the | Sets and Venn diagram | - PARCC Lesson 18: |
| probability that a girl will be | lesson and activity: | Practice Type I items - |
| selected. | http://www.shodor.org/int | Statistics and Probability |
| b. Develop a probability | eractivate/lessons/SetsThe | domain |
| model (which may not be | VennDiagram/ | - CCSS Lesson Plan: |
| uniform) by observing | (CRP2, RH.6-8.7) | Likely or Unlikely |
| frequencies in data |  | - CCSS Lesson Plan: |
| generated from a chance | Additional texts: | Test the Theory |
| process. For example, find | www.newsela.com | - CCSS Prescriptive |
| the approximate probability | www.readworks.org | Lesson Plan: The |
| that a spinning penny will | www.commonlit.org | Likelihood of Simple |
| land heads up or that a tossed |  | Events |
| paper cup will land open-end |  | - CCSS Prescriptive |
| down. Do the outcomes for |  | Lesson Plan: Large |
| the spinning penny appear to |  | Scale Probability |
| be equally likely based on the observed frequencies? |  | Outcomes |
|  |  | - CCSS Prescriptive Lesson Plan: |
|  |  | Probabilities of |
| of compound events using organized lists, tables, tree |  | Compound Events |
| diagrams, and simulation. |  | $7{ }^{\text {th }}$ grade assessments, |
| a. Understand that, just as with simple events, the |  | interactive, videos, games, |
| with simple events, the probability of a compound |  | lessons, homework: |
| event is the fraction of |  | https://www.opened.com/sea |
| outcomes in the sample |  | $\xrightarrow[\text { rch?area=mathematics\&grad }]{\text { e=7\&offset=0\&resource typ }}$ |
| space for which the |  | $\mathrm{e}=$ interactive-assessment |
| compound event occurs. |  |  |
| b. Represent sample spaces for compound events using |  | (CRP2, CRP4, CRP8, |
| methods such as organized |  | 8.1.8.A.1) |
| lists, tables and tree |  | $7{ }^{\text {th }}$ grade worksheets, |
| diagrams. For an event described in everyday |  | games, lessons, activities: |
| described in everyday language (e.g., "rolling |  | https://www.education.com/r |
| language (e.g., 'rolling |  | esources/math/middle- |



## Key Vocabulary:

## Chapter 8:

Center, radius, radii, diameter, circumference, arc, semicircle, quadrant

## Chapter 9 :

stem-and leaf plot, stem, leaf, population, sample, sample size, random sample, unbiased/biased, sample, simple random/stratified/systematic random sampling, inference

## Chapter 10:

Outcome, sample space, event, probability, fair, biased, Venn diagram, mutually exclusive, complementary events, complement, relative frequency, observed frequency, experimental probability, theoretical probability, probability model, probability distribution, uniform probability model, nonuniform probability model,

## NJ Learning Standards Vocabulary:

7.G.A. 3

Draw, construct, and describe geometrical figures and describe the relationships between them. scale drawing, dimensions, scale factor, plane sections, right rectangular prism, right rectangular pyramids, parallel, perpendicular, scalene triangle, obtuse

## 7.G.B. 4 \& 6

Solve real-life and mathematical problems involving angle measure, area, surface area, and volume inscribed, circumference, radius, diameter, pi, $\Pi$, pyramids, face, base

## 7.SP.A. 1 \& 2

Use random sampling to draw inferences about a population.
random sampling, population, representative sample, inferences

## 7.SP.B. 3 \& 4

Draw informal comparative inferences about two populations.
variation/variability distribution, measures of center, measures of variability

## 7.SP.C.5, 6, 7, \& 8

Investigate chance processes and develop, use, and evaluate probability models.
sample spaces

## Accommodations and Modifications:

Students with special needs: Support staff will be available to aid students related to IEP specifications. 504 accommodations will also be attended to by all instructional leaders. Modifications, alternative assessments, and scaffolding strategies will be used to support this learning. The use of Universal Design for Learning (UDL) will be considered for all students as teaching strategies are considered. Additional staff should be included so all students can fully participate in the standards associated with this curriculum.

ELL/ESL students: Students will be supported according to the recommendations for "can do's" as outlined by WIDA -
https://www.wida.us/standards/CAN_DOs/
Students at risk of school failure: Formative and summative data will be used to monitor student success at first signs of failure. Student work will be reviewed to determine support. This may include parent consultation, basic skills review and differentiation strategies. With considerations to UDL, time may be a factor in overcoming developmental considerations. More time will be made available with a certified instructor to aid students in reaching the standards.

Gifted and Talented Students: Students excelling in mastery of standards will be challenged with complex, high level challenges.

English Language Learners:

- Group similar problems together
- Teaching modeling
- Peer modeling
- Word walls
- Give directions in small steps and in as few words as possible
- Provide visual aids
- Group similar problems together
- Repeat directions when necessary
- Provide a vocabulary list with definitions
- Use of alge-tiles when needed
- Use of number line when needed

Special Education:

- Create a math journal that they can use during class, on assignments and (if teacher allows) on assessments
- Utilize modifications \& accommodations delineated in the students' IEP
- Work with paraprofessional
- Work with a partner
- Shorten assignments to focus on mastery or key concepts
- Maintain adequate space between desks
- Keep workspaces clear of unrelated materials
- Provide fewer problems to attain passing grades
- Tape a number line to the student's desk
- Provide extra time to complete a task when needed
- Provide definitions of different graphs / charts with illustrations
- Allow tests to be taken in a separate room
- Allow students to use a calculator when appropriate
- Divide test into small sections of similar questions or problems


## At-Risk:

- Create a math journal that they can use during class, on assignments and (if teacher allows) on assessments
- Use visual demonstrations, illustrations and models
- Give directions / instructions verbally and in simple written format
- Peer support
- Increased one - on - one

Gifted and Talented:

- Inquiry based instruction
- Independent study
- Higher order thinking skills
- Adjusting the pace of the lessons
- Real world scenarios
- Student driven instruction
- Allow students to complete an independent project as an alternative test
- Teachers may modify instructions by modeling what the student is expected to do
- Instructions may be printed out in large print and hung up for the students to see during the time of the lesson
- Review behavior expectations and make adjustments
- Allow students to complete an independent project as an alternative test
- Use of alge-tiles when needed
- Use of number line when needed

|  | $\bullet$ <br> Use of alge-tiles when <br> needed <br> - Use of number line when <br> needed |  |  |
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## Interdisciplinary Connections: ELA

NJSLSA.R1. Read closely to determine what the text says explicitly and to make logical inferences and relevant connections from it; cite specific textual evidence when writing or speaking to support conclusions drawn from the text.
NJSLSA.W2. Write informative/explanatory texts to examine and convey complex ideas and information clearly and accurately through the effective selection, organization, and analysis of content
NJSLSA.L1. Demonstrate command of the conventions of standard English grammar and usage when writing or speaking
Integration of Technology Standards NJSLS:
8.1.8.A.1: Demonstrate knowledge of a real world problem using digital tools.
$21^{\text {st }}$ Century Standards
9.2.8.B.3: Evaluate communication, collaboration and leadership skills that can be developed through school, home, work, and extracurricular activities for use in a career.

Career Ready Practices:
CRP2: Apply appropriate academic and technical skills
CRP4: Communicate clearly and effectively and with reason
CRP6: Demonstrate creativity and innovation
CRP8: Utilize critical thinking to make sense of problems and persevere in solving them

## History / Social Studies:

RH.6-8.7 Integrate visual information (e.g., in charts, graphs, photographs, videos or maps) with other information in print and digital texts

