## Englewood Public School District <br> Mathematics <br> Grade 6 <br> Second Marking Period

## Unit - Ratio, Rates and Percents

Overview: During this unit, students will learn about ratio, rates, percents and algebraic expressions.
Time Frame: Chapter 4-14 days, Chapter 6-7 days, Chapter 7-15 days

## Enduring Understandings:

You can use a ratio to compare two quantities, and you can use ratios to solve problems.
Percent is a concept used to compare quantities expressed per hundred.
Algebraic expressions can be used to describe and solve real-world problems.

## Essential Questions:

What is a ratio?
How can a ratio be used to compare two quantities?
How is a table used to show equivalent ratios?
How can you use tables to compare ratios?
How do you convert units of measure using ratios?
How are rates and percents similar?
How do rates and percents differ?
How are verbal models translated into mathematical expressions?
In a given expression, can the mathematical terms be identified?
How is the Order of Operations used in evaluating variable expressions that contain exponents?
How do properties of operations help prove expressions are equivalent?
When are expressions equivalent?

| Standards | Topics and Objectives |  | Activities |  | Resources |
| :--- | :--- | :--- | :--- | :--- | :--- |



| associated with a ratio $a: b$ with $b \neq 0$, and use rate | /ratio-and-proportionlessons.html | e=interactive-assessment <br> (CRP2, CRP4, CRP8, | unit (RH.6-8.7) |
| :---: | :---: | :---: | :---: |
| language in the context of a ratio relationship. For | - Leg task: <br> http://kuna6th.wee | 8.1.8.A.1) |  |
| example, "This recipe has a | bly.com/uploads/1/ | $6^{\text {th }}$ grade worksheets, games, lessons, activities: https://www.education.com/r | Create a dictionary defining and illustrating vocabulary terms (RH.6-8.7) |
| ratio of 3 cups of flour to 4 | 7/3/2/17324544/le |  |  |
| cups of sugar, so there is 3/4 | gs_task.pdf |  |  |
| cup of flour for each cup of | Foodbank: | esources/math/middle- |  |
| sugar." "We paid \$75 for 15 | http://kuna6th.wee | school/ | Create posters illustrating the main objectives of the unit <br> (RH.6-8.7) |
| hamburgers, which is a rate | bly.com/uploads/1/ | (CRP2, CRP4, CRP8, |  |
| of \$5 per hamburger." | 7/3/2/17324544/fo | 8.1.8.A.1) |  |
| (Expectations for unit rates | odbank_task.pdf |  |  |
| in this grade are limited to non-complex fractions.) | - Grocery store: http://kuna6th.wee bly.com/uploads/1/ | $6^{\text {th }}$ grade worksheets: <br> https://www.k5learning.com/ <br> free-math-worksheets/sixth- | Create displays of prime factorizations (RH.6-8.7) |
| 6.RP.A.3. Use ratio and rate reasoning to solve real- | 7/3/2/17324544/al | grade-6 <br> (CRP2, CRP4, CRP8) |  |
| world and mathematical | $\begin{aligned} & \text { bertson } \\ & \text { ds.pdf } \end{aligned}$ |  | Ratio design challenge: http://www.scholastic.com /unexpectedmath/ratio-challenge/teachersguide.htm (CRP2, CRP4, CRP8, RH.6-8.7) |
| problems, e.g., by reasoning about tables of equivalent | - Cookie task: http://kuna6th.wee | $6^{\text {th }}$ grade common core worksheets: |  |
| ratios, tape diagrams, double number line | $\frac{\text { bly.com/uploads/1/ }}{7 / 3 / 2 / 17324544 / c 0}$ | https://www.ixl.com/math/gr ade-6 |  |
| diagrams, or equations. | okie_task.pdf | (CRP2, CRP4, CRP8 |  |
| b. Solve unit rate problems including those involving unit pricing and constant speed. For example, if it took | - Dog food task: http://kuna6th.wee bly.com/uploads/1/ | Khan Academy - videos, lessons, assessments www.khanacademy.org |  |
| 7 hours to mow 4 lawns, then | g_food_task.pdf | (8.1.8.A.1) |  |
| at that rate, how many lawns could be mowed in 35 hours? | (CRP2, CRP4, CRP8, NJSLSAR1 |  |  |
| At what rate were lawns | NJSLSA.W2, |  |  |
| being mowed? | NJSLSA.L1) |  |  |
| Mathematical Practices MP.1, MP.2, MP.3, MP. 4 | Ratio design challenge: http://www.scholastic.com |  |  |
| MP.5, MP.6, MP.7, MP. 8 | /unexpectedmath/ratio-challenge/teachers- |  |  |
|  | guide.htm |  |  |


|  |  |  |  |
| :--- | :--- | :--- | :--- |


| Mathematical Practices | The students will be able to: <br> - Understand percent notation. <br> - Write equivalent fractions, decimals, and percents. <br> - Write more equivalent fractions, decimals and percents. <br> - Find the percent of a number. <br> - Reinforce, consolidate, and extend chapter skills and concepts. | $\underline{8}$ | Development Videos |  |
| :---: | :---: | :---: | :---: | :---: |
| MP.1, MP.2, MP.3, MP. 4 |  |  |  | Math in Focus |
| MP.5, MP.6, MP.7, MP. 8 |  | Brain Genie | North Carolina Dept of Ed. | Assessments |
|  |  | http://braingenie.ck12.org/ | Wikispaces: <br> http://maccss.ncdpi.wikispa | (Skip lessons 6.4 \& 6.5) |
|  |  | Math Game Time | ces.net/Middle+School | SE/TE: pp. 215, |
|  |  | http://www.mathgametim |  | 216-217, Items: |
|  |  | e.com/ | Math Goodies - Math | 1-14, 117-18 |
|  |  |  | Lessons |  |
|  |  | Everything you need to | http://www.mathgoodies.co | Assessments Course 1: |
|  |  | know about math | $\underline{\mathrm{m} /}$ | Chapter 6 |
|  |  | journals: |  | Test A pp. 51-53, |
|  |  | https://thecornerstoneforte | Standards Solution | Items: 1-7; |
|  |  | achers.com/math-journals/ | Lessons: | Test B pp. 54-56, |
|  |  | (NJSLSA.R1, | CCSS Lesson Plan: | Items: 1-7 |
|  |  | NJSLSA.W2, | Percent: Part of a Whole |  |
|  |  | NJSLSA.L1) |  | ExamView Assessment |
|  |  |  | $6^{\text {th }}$ grade assessments, | Suite - Test and Practice |
|  |  | Dunk tank - fractions, decimals and percents: | interactive, videos, games, lessons, homework: | Generator |
|  |  | https://wvia.pbslearningm | https://www.opened.com/sea | Alternative Assessments: |
|  |  | edia.org/resource/f79f8bb | rch?area=mathematics\&grad | Learning centers: each |
|  |  | 4-ef77-4ca5-afa8- | e=6\&offset=0\&resource_typ | learning center focuses on |
|  |  | 4e5c69211786/f79f8bb4- | e=interactive-assessment | a different type of |
|  |  | ef77-4ca5-afa8- | (CRP2, CRP4, CRP8, | problem (CRP8) |
|  |  | 4e5c69211786 | 8.1.8.A.1) |  |
|  |  | (8.1.8.A.1) |  | Create posters illustrating |
|  |  | Conversions rock - | $6^{\text {th }}$ grade worksheets, games, lessons, activities: | the main objectives of the unit |
|  |  | lessons and activities: <br> https://www.scholastic.co | https://www.education.com/r esources/math/middle- |  |
|  |  | m/teachers/sponsored- | school/ | Create a dictionary |
|  |  | content/unexpected- | (CRP2, CRP4, CRP8, | defining and illustrating |
|  |  | math/17-18/conversions- | 8.1.8.A.1) | vocabulary terms |
|  |  | rock/ |  | (RH.6-8.7) |
|  |  | (CRP2, CRP8) | $6^{\text {th }}$ grade worksheets: <br> https://www.k5learning.com/ | Create posters illustrating |
|  |  | Additional texts: | free-math-worksheets/sixth- | the main objectives of the |



| Chapter 7 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 6.EE.A.2. Write, read, and evaluate expressions in which letters stand for numbers. <br> a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5" as $5-y$. <br> b. Identify parts of an expression using mathematical terms (sum, term, product, factor, | Topics <br> Writing, evaluating, simplifying, expanding and factoring algebraic expressions. Solving realworld problems with algebraic expressions. <br> Twenty-First Century Themes and Skills include: <br> - Creativity and Innovation <br> - Critical Thinking and Problem Solving | 6.EE.A. 2 Rectangle Perimeter 1 <br> 6.EE.A. 4 Rectangle <br> Perimeter 2 <br> 6.EE.A. 4 Equivalent <br> Expressions <br> Math Playground http://www.mathplaygrou nd.com/ <br> Math Fact Practice http://www.playkidsgam | SE-6A: 221-259 <br> My HRW - Online access to all Math in Focus materials listed above and Virtual Manipulatives <br> Technology Resources <br> - Math in Focus eBooks <br> - Math in Focus Teacher Resources CD <br> - Interactive Whiteboard lessons <br> - Virtual Manipulatives | Formative Assessments: <br> Math journal <br> (NJSLSA.R1, <br> NJSLSA.W2, <br> NJSLSA.L1) <br> Multiple choice / short answer assessments (CRP8) <br> Mini quizzes - assess just one topic, or what was done within 1 or 2 days (CRP8) |

quotient, coefficient); view
one or more parts of an
expression as a single entity.
For example, describe the
expression 2(8+7) as a
product of two factors; view
(8+7) as both a single entity
and a sum of two terms
c. Evaluate expressions at
specific values of their
variables. Include
expressions that arise from
formulas used in real-world
problems. Perform
arithmetic operations,
including those involving
whole-number exponents, in
the conventional order when
there are no parentheses to
specify a particular order
(Order of Operations). For
example, use the formulas
V=s and A=6s to find the
volume and surface area of a
cube with sides of length
$s=1 / 2$.
6.EE. A. 3 . Apply the
properties of operations to
generate equivalent
expressions. For example,
apply the distributive
property to the expression 3
( $2+x$ ) to produce the
equivalent expression $6+3 x$;
apply the distributive
property to the expression
$24 x+18 y ~ t o ~ p r o d u c e ~ t h e ~$
quotient, coefficient); view one or more parts of an ntity. expression $2(8+7)$ as a product of two factors; view (8+7) as both a single entity and a sum of two terms c. Evaluate expressions at specfic values of tueir expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving the conventional order when there are no parentheses to (Oriy a particular order (Order of Operations). For example, use the formulas $V=s^{3}$ and $A=6 s^{2}$ to find the cube with sides of length $s=1 / 2$.

## 6.EE.A.3. Apply the

 properties of operations to gererate equivaient apply the distributive property to the expression 3 equivalent expression $6+3 x$; apply the distributive $24 x+18 y$ to produce the- Communication and Collaboration


## Objectives

The students will be able to:

- Use variables to write algebraic expressions.
- Evaluate algebraic expressions for given values of the variables.
- Simplify algebraic expressions in one variable.
- Recognize that the expression obtained after simplifying is equivalent to the original expression.
- Expand simple algebraic expressions.
- Factor simple algebraic expressions.
- Solve real-world problems involving algebraic expressions.
- Reinforce, consolidate, and extend chapter skills and concepts.


## es.com/games/mathfact/ mathFact.htm <br> - Online Professional Development Videos

Grades 6-8 Math Fluency Support
https://www.engageny.org /resource/mathematics-fluency-support-grades-68

## Brain Genie

http://braingenie.ck12.org/

## Math Game Time

http://www.mathgametim e.com/

## Everything you need to

know about math

## journals:

https://thecornerstoneforte
achers.com/math-journals/ (NJSLSA.R1,
NJSLSA.W2,
NJSLSA.L1)
Activities for algebraic expressions (registration required):
https://www.buzzmath.co m/badges/criteria/content-cc6-algebraic-expressionsgold
(NJSLSA.W2)
Writing algebraic expressions - lesson and activities: Wikispaces:
http://maccss.ncdpi.wikispa
ces.net/Middle+School
Math Goodies - Math

## Lessons

http://www.mathgoodies.co

## m/

## Standards Solution

Lessons:

- PARCC Lesson 8:

Equivalent Expressions

- PARCC Lesson 15:

Performance Based
Assessment - Reasoning

- CCSS Lesson Plan:

Equivalent Expression
Game

- CCSS Lesson Plan:

Variables in Expressions
$6^{\text {th }}$ grade assessments, interactive, videos, games, lessons, homework:
https://www.opened.com/sea rch?area=mathematics\&grad e=6\&offset=0\&resource_typ e=interactive-assessment (CRP2, CRP4, CRP8, 8.1.8.A.1)
$6^{\text {th }}$ grade worksheets, games, lessons, activities:

Summative Assessments:
Math in Focus
North Carolina Dept of Ed. Assessments
SE/TE: pp. 108,
109-110, 111-113

## Assessments Course 1:

## Chapter 7

Test A pp. 59-61;
Test B pp. 62-64

## Assessments Course 1:

## Mid-Course Test A

pp. 65-72;
Mid-Course Test B
pp. 73-80
ExamView Assessment Suite - Test and Practice Generator

## Alternative Assessments:

Learning centers: each learning center focuses on a different type of problem (CRP8)

Create posters illustrating the main objectives of the unit (RH.6-8.7)

Create a dictionary defining and illustrating vocabulary terms (RH.6-8.7)

| equivalent expression 6 ( $4 x+$ | https://betterlesson.com/le | https://www.education.com/r |  |
| :---: | :---: | :---: | :---: |
| $3 y)$; apply properties of | sson/544062/writing- | esources/math/middle- | Create posters illustrating |
| operations to $y+y+y$ to | algebraic-expressions | school/ | the main objectives of the |
| produce the equivalent expression $3 y$. | (NJSLSA.W2) | (CRP2, CRP4, CRP8, 8.1.8.A.1) | $\begin{aligned} & \text { unit } \\ & \text { (RH.6-8.7) } \end{aligned}$ |
| 6.EE.A.4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y+y+y$ and $3 y$ are equivalent because they name the same number regardless of which number $y$ stands for. | Algebraic expressions |  |  |
|  | and the real world - lesson and activities: | $6^{\text {th }}$ grade worksheets: <br> https://www.k5learning.com/ | Create displays of prime factorizations |
|  | https://betterlesson.com/le | free-math-worksheets/sixth- | (RH.6-8.7) |
|  | sson/544063/algebraic- | grade-6 |  |
|  | expressions-and-the-real- | (CRP2, CRP4, CRP8) | Have students create their |
|  | (NJSLSA.W2) | $6^{\text {th }}$ grade common cor | based on the website |
|  |  | worksheets: | below and share them |
|  | Algebraic expressions with dots: | https://www.ixl.com/math/gr ade-6 | with the class / a partner: https://labyrinth.thinkport. |
|  | https://labyrinth.thinkport. | (CRP2, CRP4, CRP8 | org/www/educators/resour |
|  | org/www/educators/resour |  | ces/lessons/lounge_grade6 |
|  | ces/lessons/lounge_grade6 | Khan Academy - videos, | .pdf |
| 6.EE.B.6. Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set. | .pdf | lessons, assessments | (RH.6-8.7, CRP6, CRP8) |
|  | (CRP6, CRP8, | www.khanacademy.org |  |
|  | NJSLSA.W2) | (8.1.8.A.1) |  |
|  |  |  |  |
|  | Additional texts: |  |  |
|  | www.newsela.com |  |  |
|  | www.readworks.org |  |  |
|  | www.commonlit.org |  |  |
|  |  |  |  |
| Mathematical Practices MP.1, MP.2, MP.3, MP. 4 MP.6, MP. 7 |  |  |  |
|  |  |  |  |
|  |  |  |  |

## Key Vocabulary:

## Chapter 4:

ratio, term, equivalent ratios, simplest form

## Chapter 6:

percent

## Chapter 7:

Variable, algebraic expression, terms, evaluate, substitute, simplify, coefficient, like terms, equivalent expressions, expand, factor

## NJ Learning Standards Vocabulary:

## 6.RP.A.1, 2, \& 3

Understand ratio concepts and use ratio reasoning to solve problems.
ratio, equivalent ratios, tape diagram, unit rate, part-to-part, part-to-whole, percent

## 6.EE.A. 2, 3, \& 4

Apply and extend previous understanding of arithmetic to algebraic expressions.
exponents, base, numerical expressions, algebraic expressions, evaluate, sum, term, product, factor, quantity, quotient, coefficient, constant, like terms, equivalent expressions, variables

## 6.EE.B. 6

Reason about and solve one-variable equations and inequalities.
inequalities, equations, greater than, $>$, less than, $<$, greater than or equal to, $\geq$, less than or equal to, $\leq$, profit, exceed

## Accommodations and Modifications:

Students with special needs: Support staff will be available to aid students related to IEP specifications. 504 accommodations will also be attended to by all instructional leaders. Modifications, alternative assessments, and scaffolding strategies will be used to support this learning. The use of Universal Design for Learning (UDL) will be considered for all students as teaching strategies are considered. Additional staff should be included so all students can fully participate in the standards associated with this curriculum.

ELL/ESL students: Students will be supported according to the recommendations for "can do's" as outlined by WIDA -
https://www.wida.us/standards/CAN_DOs/
Students at risk of school failure: Formative and summative data will be used to monitor student success at first signs of failure. Student work will be reviewed to determine support. This may include parent consultation, basic skills review and differentiation strategies. With considerations to UDL, time may be a factor in overcoming developmental considerations. More time will be made available with a certified instructor to aid students in reaching the standards.

Gifted and Talented Students: Students excelling in mastery of standards will be challenged with complex, high level challenges.

English Language Learners:

- Teaching modeling
- Peer modeling
- Word walls
- Give directions in small steps and in as few words as possible
- Provide visual aids
- Group similar problems together
- Repeat directions when necessary
- Provide a vocabulary list with definitions

Special Education:

- Utilize modifications \& accommodations delineated in the students' IEP
- Work with paraprofessional
- Work with a partner
- Shorten assignments to focus on mastery or key concepts
- Maintain adequate space between desks
- Keep workspaces clear of unrelated materials
- Provide fewer problems to attain passing grades
- Tape a number line to the student's desk
- Create a math journal that they can use during class, on assignments and (if teacher allows) on assessments
- Provide extra time to complete a task when needed
- Provide definitions of different graphs / charts with illustrations
- Allow tests to be taken in a separate room
- Allow students to use a calculator when appropriate
- Divide test into small sections of similar questions or problems


## At-Risk:

- Use visual demonstrations, illustrations and models
- Give directions / instructions verbally and in simple written format
- Peer support
- Increased one - on - one time
- Teachers may modify instructions by modeling what the student is expected to do
- Instructions may be printed out in large print and hung up for the students to see during the time of the lesson
- Review behavior expectations and make adjustments
- Create a math journal that they can use during class, on assignments and (if teacher allows) on assessments
- Allow students to complete an independent project as an alternative test


## Gifted and Talented:

- Inquiry based instruction
- Independent study
- Higher order thinking skills
- Adjusting the pace of the lessons
- Real world scenarios
- Student driven instruction
- Allow students to complete an independent project as an alternative test

NJSLSA.R1. Read closely to determine what the text says explicitly and to make logical inferences and relevant connections from it; cite specific textual evidence when writing or speaking to support conclusions drawn from the text.
NJSLSA.W2. Write informative/explanatory texts to examine and convey complex ideas and information clearly and accurately through the effective selection, organization, and analysis of content
NJSLSA.L1. Demonstrate command of the conventions of standard English grammar and usage when writing or speaking
RH.6-8.7 Integrate visual information (e.g., in charts, graphs, photographs, videos or maps) with other information in print and digital texts

## Integration of Technology Standards NJSLS:

8.1.8.A.1: Demonstrate knowledge of a real world problem using digital tools.

## $21^{\text {st }}$ century standards

9.2.8.B.1: Research careers within the 16 Career Clusters and determine attributes of career success.
9.2.8.B.2: Develop a Personalized Student Learning Plan with the assistance of an adult mentor that includes information about career areas of interest, goals and an educational path.
9.2.8.B.3: Evaluate communication, collaboration and leadership skills that can be developed through school, home, work, and extracurricular activities for use in a career.

## Career Ready Practices:

CRP2: Apply appropriate academic and technical skills
CRP4: Communicate clearly and effectively and with reason
CRP6: Demonstrate creativity and innovation
CRP8: Utilize critical thinking to make sense of problems and persevere in solving them

